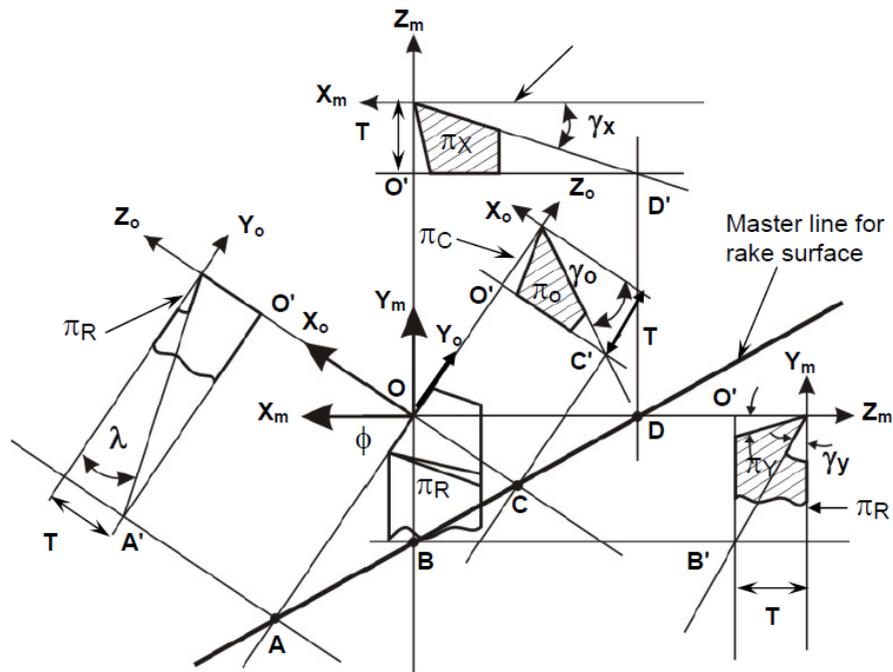


# Conversion of Angles by Graphical Method

## 2.4.1.1. Conversion of angles of single point tools by graphical method

### Conversion of rake angles

The concept and construction of ML for the tool rake surface is shown in Fig



In Fig, the rake surface, when extended along  $\pi_x$  plane, meets the tool's bottom surface (which is parallel to  $\pi_R$ ) at point  $D'$  i.e.  $D$  in the plan view. Similarly when the same tool rake surface is extended along  $\pi_y$ , it meets the tool's bottom surface at point  $B'$  i.e., at  $B$  in plan view. Therefore, the straight line obtained by joining  $B$  and  $D$  is nothing but the line of intersection of the rake surface with the tool's bottom surface which is also parallel to  $\pi_R$ . Hence, if the rake surface is extended in any direction, its meeting point with the tool's bottom plane must be situated on the line of intersection, i.e.,  $BD$ . Thus the points  $C$  and  $A$  (in Fig. 4.1) obtained by extending the rake surface along  $\pi_o$  and  $\pi_c$  respectively upto the tool's bottom surface, will be situated on that line of intersection,  $BD$ .

This line of intersection,  $BD$  between the rake surface and a plane parallel to  $\pi_R$  is called the "Master line of the rake surface".

From the diagram in Fig.

$$OD = T \cot \gamma_x$$

$$OB = T \cot \gamma_y$$

$$OC = T \cot \gamma_o$$

$$OA = T \cot \lambda$$

Where, T = thickness of the tool shank.

## Conversion of tool rake angles from ORS to ASA

$\alpha_o$  and  $\lambda$  (in ORS) = f ( $\gamma_x$  and  $\gamma_y$  of ASA system)

Proof of Equation 4.1:

With respect to Fig. 4.2,

Consider,  $\Delta OBD = \Delta OBC + \Delta OCD$

Or,  $\frac{1}{2} OB \cdot OD = \frac{1}{2} OB \cdot CE + \frac{1}{2} OD \cdot CF$

Or,  $\frac{1}{2} OB \cdot OD = \frac{1}{2} OB \cdot OC \sin \phi + \frac{1}{2} OD \cdot OC \cos \phi$

Dividing both sides by  $\frac{1}{2} OB \cdot OD \cdot OC$ ,

$$1/OC = 1/OD \sin(\phi) + 1/OB \cos(\phi)$$

Similarly Equation 4.2 can be proved considering;

$\Delta OAD = \Delta OAB + \Delta OBD$

i.e.,  $\frac{1}{2} OD \cdot AG = \frac{1}{2} OB \cdot OG + \frac{1}{2} OB \cdot OD$

where,  $AG = OA \sin \phi$

and  $OG = OA \cos \phi$

Now dividing both sides by  $\frac{1}{2} OA \cdot OB \cdot OD$ ,

$$1/OB \sin \phi = 1/OD \cos \phi + 1/OA$$

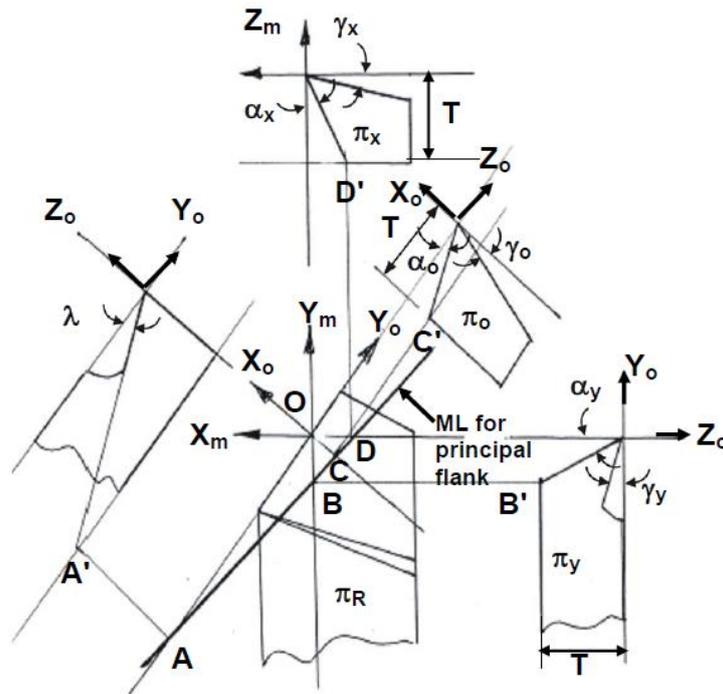
Fig.2.24

## Conversion of clearance angle

### Conversion of clearance angles from ASA to ORS

Angles,  $\alpha_o$  and  $\lambda$  in ORS = f ( $\alpha_x$  and  $\alpha_y$  in ASA system)

Following the same way used for converting the rake angles taking suitable triangles (in Fig. 4.2), the following expressions can be arrived at using Fig



Conversion of clearance angles from ORS to ASA system

$$\alpha_x \text{ and } \alpha_y \text{ (in ASA)} = f(\alpha_o \text{ and } \lambda \text{ in ORS})$$

Proceeding in the same way using Fig. 4.5, the following expressions are derived

$$\cos\phi \sin\phi \cot\alpha_x \cot\lambda \tan\phi = \dots \quad (4.14)$$

$$\text{and } \sin\phi \cos\phi \cot\alpha_y \cot\lambda \tan\phi = \dots \quad (4.15)$$

The relations (4.14) and (4.15) are also possible to be attained from inversions of Equation 4.13 as indicated in case of rake angles.

## Determination of minimum clearance and setting angle

Minimum clearance,  $\alpha_{\min}$  or  $\alpha_m$

The magnitude and direction of minimum clearance of a single point tool may be evaluated from the line segment OM taken normal to the Master line (Fig. 4.5) as  $OM = \tan\alpha_m$

The values of  $\alpha_m$  and the orientation angle,  $\phi_\alpha$  (Fig. 4.5) of the principal flank are useful for conveniently grinding the principal flank surface to sharpen the principal cutting edge.

Proceeding in the same way and using Fig. 4.5, the following expressions could be developed to evaluate the values of  $\alpha_m$  and  $\phi_\alpha$

Similarly the clearance angles and the grinding angles of the auxiliary flank surface can also be derived and evaluated.

o Interrelationship amongst the cutting angles used in ASA and ORS

The relations are very simple as follows:

$$\phi \text{ (in ORS)} = 90^\circ - \phi_s \quad \text{(in ASA) (4.20)}$$

$$\text{and } \phi_1 \text{ (in ORS)} = \phi_e \quad \text{(in ASA) (4.21)}$$